

**DIFFERENTIATION**

**INTEGRATION**

(constants of integration omitted)

Function	Derivative	Function	Integral
$x^n$	$nx^{n-1}$	$x^n$	$\frac{x^{n+1}}{n+1} (n \neq -1)$
$(ax+b)^n$	$an(ax+b)^{n-1}$	$(ax+b)^n$	$\frac{(ax+b)^{n+1}}{a(n+1)} (n \neq -1)$
$(f(x))^n$	$n(f(x))^{n-1} f'(x)$	$f'(x)(f(x))^n$	$\frac{(f(x))^{n+1}}{n+1} (n \neq -1)$
$\ln x$	$\frac{1}{x}$	$\frac{1}{x}$	$\ln x $
$\ln(ax+b)$	$\frac{a}{ax+b}$	$\frac{1}{ax+b}$	$\frac{1}{a} \ln(ax+b)$
$\ln(f(x))$	$\frac{f'(x)}{f(x)}$	$\frac{f'(x)}{f(x)}$	$\ln f(x) $
$e^x$	$e^x$	$e^x$	$e^x$
$e^{ax+b}$	$ae^{ax+b}$	$e^{ax+b}$	$\frac{1}{a} e^{ax+b}$
$e^{f(x)}$	$f'(x)e^{f(x)}$	$f'(x)e^{f(x)}$	$e^{f(x)}$
<b>Note: Calculus involving trig functions assumes you are working in RADIANS</b>			
$\sin x$	$\cos x$	$\cos x$	$\sin x$
$\cos x$	$-\sin x$	$\sin x$	$-\cos x$
$\tan x$	$\sec^2 x$	$\sec^2 x$	$\tan x$
$\sin(ax+b)$	$a \cos(ax+b)$	$\cos(ax+b)$	$\frac{1}{a} \sin(ax+b)$
$\sin(f(x))$	$f'(x) \cos(f(x))$	$f'(x) \cos(f(x))$	$\sin(f(x))$
similarly for cos and tan		similarly for sin and sec <sup>2</sup>	
$uv$ Product Rule	$v \frac{du}{dx} + u \frac{dv}{dx}$	$u \frac{dv}{dx}$ Integration by parts	$uv - \int v \frac{du}{dx} dx$
$\frac{u}{v}$ Quotient Rule	$\frac{v \frac{du}{dx} - u \frac{dv}{dx}}{v^2}$	$\cos^2 x$	Use double angle formula $\cos^2 x = \frac{1}{2} + \frac{1}{2} \cos 2x$
$x = f(t), y = g(t)$ Parametric differentiation	$\frac{dy}{dx} = \frac{dy}{dt} \div \frac{dx}{dt}$	$\sin^2 x$	Use double angle formula $\sin^2 x = \frac{1}{2} - \frac{1}{2} \cos 2x$
$y = f(u), u = g(x)$ Chain Rule	$\frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx}$	Method of substitution: <b>1.</b> substitute for dx in terms of du <b>2.</b> substitute for x in terms of u <b>3.</b> change limits to u Always look for simplifications before the next stage.	
Useful Relation	$\frac{dy}{dx} = 1 \div \frac{dx}{dy}$	General method: <b>1.</b> Is it a standard integral? <b>2.</b> Is it a reverse chain rule?(can you spot a function and its derivative?) <b>3.</b> Can you split it up into two or more easier integrals? e.g. $\int \frac{x+1}{x} dx = \int 1 + \frac{1}{x} dx$ . <b>4</b> Can you use partial fractions? <b>5.</b> Can you use a trig formula? <b>6.</b> Can you do it by parts? <b>7.</b> Can you use a substitution? More than one method may work; which is the easiest?	

**Warning:** You cannot differentiate or integrate the parts of a product or quotient separately: consider multiplying or dividing out first or using another method.